

2018 ICPC Southeast USA Regional Contest

Count the Bits

Given a value k and a number of bits b , calculate the total number of 1-bits in the binary representations of all multiples of k that are between 0 and 2^b-1 (inclusive).

Input

Each input will consist of a single test case. Note that your program may be run multiple times on different inputs.

Each test case will consist of a single line containing two space-separated integers k ($1 \leq k \leq 1,000$) and b ($1 \leq b \leq 128$), where k and b are as described above.

Output

Output a single integer, which is the total number of 1-bits in the binary representations of all multiples of k that are between 0 and 2^b-1 (inclusive). Since this number may be very large, output it modulo 10^9+9 .

Sample Input	Sample Output
1 4	32
10 5	8
100 7	3
3 28	252698795
11 128	856188165
1 26	872415232
876 128	530649653

Consider the second sample: $k=10$ and $b=5$.

$2^5-1 = 31$. All the multiples of 10 between 0 and 31 are: 10, 20 and 30.

10 = 01010b (2 1-bits)

20 = 10100b (2 1-bits)

30 = 11110b (4 1-bits)

That's a total of $2+2+4=8$ 1-bits.